# KDL

## **Causal Graphs vs. Causal Programs** The Case of Conditional Branching Sam Witty and David Jensen



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## . Motivation

**Causal models** extend purely probabilistic models, enabling reasoning about joint distributions of random variables in the presence of well-defined interventions[2].

**Causal probabilistic programs** include common programming constructs such as recursion, looping, and conditional branching. Conditional branching[1] can be used to represent **context-dependent** causal structure, i.e. for some subset of random variables, C, there exist two execution paths i and j through the program, such that  $Pa(C_i) \neq Pa(C_j)$ .

A set of techniques has been developed over the past 25 years to learn the structure of causal graphical models from observational (non-experimental) data[3], however they implicitly assume that the graph structure is **context-independent**.

**Program P1:** Context-Independent Structure

## 3. Structure Discovery Experiments

We evaluate the performance of graph-based structure discovery algorithms when the generative process is a causal probabilistic program with context-dependent causal structure using synthetic experiments.

To do this we: (1) generate observational samples from programs P1 and P2, (2) learn a Markov equivalence class of graphical models using the max-min hill climbing algorithm[4], (3) non-parametrically estimate local conditional probability distributions, and (4) generate interventional samples from both the causal probabilistic program and the learned graphical model for the intervention do(A = a).







When the generative process is not interventionally equivalent to any causal graphical) model, the graph-based causal discovery procedure produces estimates that closely approximate the observational distribution, but deviate significantly from the interventional distribution.

Given a probabilistic program with context-dependent causal structure there does not exist an interventionally equivalent causal graphical model. However, there may exist an observationally equivalent causal graphical model.

### 4. Conclusions

- We demonstrate that simple causal probabilistic programs with conditional branching can represent causal processes that are not learned effectively by the most common algorithms for learning causal graphical models.
- This is despite the fact that the same learning procedures produce observational estimates that closely approximate the programs' observational distribution.
- The task of learning the structure of causal models with context-dependent causal structure remains an important research frontier.

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